

A Recollection on Probability

Average Value

- ❖ The Average Value (or Mean Value) of a set of '**N**' values $x_1, x_2, \dots, x_n$ of '**x**' is denoted by either **x** or $\langle x \rangle$ and is given by

$$\bar{x} = \langle x \rangle = \frac{x_1 + x_2 + \dots + x_N}{N} = \frac{1}{N} \sum_{j=1}^N x_j$$

- ❖ The Summation is over all the '**N**' values of x_j 's.

- For example, if the values x_j , are 6,7,6,7,7,8,9,7,5,8 the average value of ' x ' is

$$\bar{x} = \langle x \rangle = \frac{(6+7+6+7+7+8+9+7+5+8)}{10} = 7$$

- Since there are **five, two sixes, four sevens, two eights** and **one nine**, the expression for ' x ' can be written in the form

$$\bar{x} = \frac{(1 \times 5 + 2 \times 6 + 4 \times 7 + 2 \times 8 + 1 \times 9)}{10}$$

$$= \frac{1}{10} \times 5 + \frac{2}{10} \times 6 + \frac{4}{10} \times 7 + \frac{2}{10} \times 8 + \frac{1}{10} \times 9$$

Probability of getting a 5 = $\frac{1}{10}$

Probability of getting a 6 = $\frac{2}{10}$ and so on

$$\therefore \bar{x} = \langle x \rangle = \sum_i x_i P_i$$

Probability of getting the value of x_i

Microstates and Macrostates

Microstates	Possible arrangement in compartment 1	Possible arrangement in compartment 2	No. of Microstates
(0,4)	0	abcd	1
(1,3)	a b c d	bcd acd abd abc	4
(2,2)	ab ac ad bc db cd	cd bd bc ad ac ab	6
(3,1)	bcd acd abd abc	a b c d	4
(4,0)	abcd	0	1